CE272

## Fluid Mechanics Sessional （Lab Manual）



# Department of Civil Engineering Ahsanullah University of Science and Technology 

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## Preface

Fluid mechanics is an undergraduate subject for civil engineers which basically deals with fluids (water). Different equations and formulas are there to calculate the discharge, velocity etc of fluids and many other techniques are available which all are discussed under this subject. This Lab manual mainly deals with the common and universal laboratory tests of Fluid (water). Centre of Pressure, Proof of Bernoulli's theorem, Flow through Venturimeter, Flow through orifice, Flow through mouthpiece, Flow over V-notch, Flow over sharp crested weir, Fluid friction in pipe, Head loss due to sudden expansion and sudden contraction of pipe.

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## Experiment 1 <br> Centre of Pressure



## CE 272: Fluid Mechanics Sessional <br> Experiment No. 1 <br> Centre of Pressure

## General

The centre of pressure is a point on the immersed surface at which the resultant of liquid pressure force acts. In case of horizontal area the pressure is uniform and the resultant pressure force passes through the centroid of the area, but for an inclined surface this point lies towards the deeper end of the surface, as the intensity of pressure increases with depth.

The objective of this experiment is to locate the centre of pressure of an immersed rectangular surface and to compare this position with that predicted by theory.

## Practical Application

For structural design of water control gates, the location and magnitude of water pressure acting on gates is imporatnt. In designing a hydraulic structure (e.g a dam) the overturning moment about O created by water pressure on the structure is required to retain the structure $\mathrm{W}^{*} \mathrm{X}$ must be more than $\mathrm{F}^{*} \mathrm{Y} . \mathrm{M}_{0}=\mathrm{F}^{*} \mathrm{Y}$, where F is the resultant force of water on the dam and Y is the distance of the centre of the pressure from bottom, W is the weight of the dam and X is the distance from center of gravity to pivot point O .


Fig 1. Practical application of centre of pressure


Fig 2. Location of the resultant force acting on a dam

## Description of Apparatus

The apparatus is comprised basically of a rectangular transparent water tank, which supports a torroidal quadrant of rectangular section complete with an adjustable counter-balance and a water level measuring device.

The Clear Perspex (acrylic resin) rectangular water tank has a drain tap at one end and a knurled levelling screw at each corner of the base. Centrally disposed at the top edge of the two long sides, are mounted on the brass knife-edge supports, immersed within the tank and pivoted at its geometric centre of curvature on the knife-edge supports, is an accurate torroidal quadrant (ring segment).This is clamped and dowelled to an aluminum counterbalance arm which has a cast-iron main weight with a knurled head brass weight for fine adjustment at one end and a laboratory type weight pan at the other end. Two spirit levels are mounted on the upper surface of the arm. The Water level is accurately indicated by a point gauge which is at one of the tank.

## Theory

The magnitude of the total hydrostatic force F will be given by

$$
F=\rho g \bar{y} \mathrm{~A}
$$

Where $\rho=$ Density of fluid
$g=$ Acceleration due to gravity
$\bar{y}=$ Depth to centroid of immersed surface
$A=$ Area of immersed surface
This force will act through the centre of pressure C.P. at a distance $y_{p}$ (Measured vertically) from point O , where O is the intersection of the plane of the water surface and the plane of the rectangular surface.

Theoretical Determination of $y_{p}$ :
Theory shows that

$$
y_{p}=\bar{y}+\frac{\mathrm{I}_{C G}}{A \bar{y}}
$$

where

$$
\begin{array}{ll}
y & = \\
\mathrm{I}_{\mathrm{CG}} & =\quad \text { distance from } \mathrm{O} \text { to the centroid } \mathrm{CG} \text { of the immersed surface. } \\
2^{\text {nd }} \text { moment of area of the immersed surface about the horizontal axis } \\
\text { through CG. }
\end{array}
$$



Fig 3. Partially submerged condition


Fig 4. Fully submerged condition

## Experimental Determination of $y_{p}$ :

For equilibrium of the experimental apparatus, moments about the pivot P give

$$
\begin{array}{rll}
\mathrm{Fy} & = & \mathrm{W} . \mathrm{z} \\
& = & \mathrm{Mg} . \mathrm{z}
\end{array}
$$

Where

$$
\begin{array}{ll}
\mathrm{y} & =\text { Distance from pivot to centre of pressure } \\
\mathrm{M} & =\text { Mass added to hanger }
\end{array}
$$

$\mathrm{z}=$ Distance from pivot to hanger
Therefore
$\mathrm{y}=\frac{M g z}{F}$
But $\mathrm{y}=y_{p}+r-y_{1} \quad$ [fully submerged]
$\mathrm{y}=y_{p}+r+y_{1} \quad$ [partially submerged]
Therefore
$y_{p} \quad=\quad \mathrm{y}-\left(\mathrm{r}-\mathrm{y}_{1}\right) \quad$ [fully submerged]
$y_{p} \quad=\quad \mathrm{y}-\left(\mathrm{r}+\mathrm{y}_{1}\right) \quad$ [partially submerged]
Where
r $\quad=\quad$ Distance from pivot to top of rectangular surface
$\mathrm{y}_{1} \quad=\quad$ Distance from water surface to top of rectangular surface
In Fig
$\mathrm{y}_{2}=$ Distance from water surface to bottom of rectangular surface

## Procedure

1. The apparatus is placed in a splash tray and correctly leveled.
2. The length $l$ and width $b$ of the rectangular surface, the distance $r$ from the pivot to the top of the surface, and the distance $s$ from the hanger to the pivot were recorded.
3. The rectangular surface is positioned with the face vertical $(\theta=0)$ and clamped.
4. The position of the moveable jockey weight is adjusted to give equilibrium, i.e. when the balance pin is removed there is no movement of the apparatus. The balance pin is replaced.
5. Water is added to the storage chamber. This created an out-of-balance clockwise moment in the apparatus. A mass M is added to the hanger and water is slowly removed from the chamber via drain hole such that the system is brought almost to equilibrium, but now clockwise moment is marginally greater. Water is slowly added to the storage chamber by a dropper until equilibrium is attained. At this condition the drain hole is closed and the balance pin again removed to cheek equilibrium.
6. The balance pin is replaced and the values of $y_{1}, y_{2}$ and $M$ were recorded.
7. The above procedure is repeated for various combinations of depth.

## Objective

1. To determine the distance of center of pressure from the water surface both theoretically and practically.
2. To plot the mass on the pan (M) against $\mathrm{y}_{2}$ in plain graph paper.

## Practice Questions

1. Discuss why the centre of pressure is below the centre of gravity for a submerged plane.
2. What are the practical applications of the centre of pressure?

## Experiment No. 1

## CENTRE OF PRESSURE

## Experimental Data Sheet

Inner radius of curvature, r
Outer radius of curvature, R
Width of plane surface, b
-

Height of Plane surface, 1
=.......................................

Distance from pivot to hanger, z

| Group <br> No. | $\mathrm{y}_{1}$ | $\mathrm{y}_{2}$ | $\bar{y}$ | F | $\mathrm{I}_{\mathrm{CG}}$ | $\frac{I_{c g}}{-\bar{y}}$ | $\mathrm{y}_{\mathrm{p}}$ <br> theo. | M | y | $\mathrm{y}_{\mathrm{p}}$ <br> exp. | submerged <br> condition |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Comment |  |  |  |  |  |  |  |  |  |  |  |


| Group No. |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Weight on pan |  |  |  |  |  |
| $\mathrm{y}_{2}$ |  |  |  |  |  |

## Experiment 2 Bernoulli's Theorem



# CE 272: Fluid Mechanics Sessional Experiment No. 2 <br> BERNOULLI'S THEOREM 

## General

Energy is the ability to do work. It manifests in various forms and can change from one form to another. These various forms of energy present in fluid flow are elevation, kinetic, pressure and internal energies. Internal energies are due to molecular agitation and manifested by temperature. Heat energy may be added to or subtracted from a flowing fluid through the walls of the tube or mechanical energy may be added to or subtracted from the fluid by a pump or turbine. Daniel Bernoulli in the year 1983 stated that in a steady flow system of frictionless (or non-viscous) incompressible fluid, the sum of pressure, elevation and velocity heads remains constant at every section, provided no energy is added to or taken out by an external source.

## Practical application

Bernoulli's Energy Equation can be applied in practice for the construction of flow measuring devices such as venturimeter, flow nozzle, orifice meter and Pitot tube, Furthermore, it can be applied to the problems of flow under a sluice gate, free liquid jet, radial flow and free vortex motion. It can also be applied to real incompressible fluids with good results in situations where frictional effect is very small.

## Description of apparatus

The unit is constructed as a single Perspex fabrication. It consists of two cylindrical reservoirs inter-connected by a Perspex Venturi of rectangular cross-section. The Venturi is provided with a number of Perspex piezometer tubes to indicate the static pressure at each cross-section. An engraved plastic backboard is fitted which is calibrated in British and Metric units. This board can be reversed and mounted on either side of the unit so that various laboratory configurations can be accommodated. The inlet vessel is provided with a dye injection system. Water is fed to the upstream tank through a radial diffuser from the laboratory main supply. For satisfactory results the mains water pressure must be nearly constant. After flowing through the venture, water is discharged through a flow-regulating device. The rate of flow through the unit may be detrimental either volumetrically or gravimetrically. The equipment for this purpose is excluded from the manufacturer's supply. The apparatus has been made so that the direction of flow through the venturi can be reversed for demonstration purpose. To do this the positions of the dye injector and discharge fitting have to be interchanged.


## SKETCH OF APPARATUS



## VENTURI DETAILS

Fig 1. Sketch of Apparatus and Venturi Details

## Governing Equation

Assuming frictionless flow, Bernoulli's Theorem states that, for a horizontal conduit

$$
Z_{1}+\frac{P_{1}}{\gamma}+\frac{V_{1}^{2}}{2 g}=Z_{2}+\frac{P_{2}}{\gamma}+\frac{V_{2}^{2}}{2 g}=Z_{3}+\frac{P_{3}}{\gamma}+\frac{V_{3}^{2}}{2 g}=\ldots \ldots .
$$

where, $\mathrm{Z}_{1}, \mathrm{Z}_{2}=\quad$ Elevation head at section 1 and 2
$\mathrm{P}_{1,}, \mathrm{P}_{2}=$ pressure of flowing fluid at sections 1 and 2
$\gamma \quad=\quad$ unit weight of fluid
$\mathrm{V}_{1}, \mathrm{~V}_{2}=\quad$ mean velocity of flow at sections 1 and 2
$\mathrm{g}=$ acceleration due to gravity.
The equipment can be used to demonstrate the validity of this theory after an appropriate allowance has been made for friction losses.

For actual condition there must be some head loss in the direction of flow. So if the head loss between section 1 and 2 is $h_{L}$ Bernoulli's theorem is modified to
$Z_{1}+\frac{P_{1}}{\gamma}+\frac{V_{1}{ }^{2}}{2 g}=Z_{2}+\frac{P_{2}}{\gamma}+\frac{V_{2}{ }^{2}}{2 g}+\mathrm{h}_{\mathrm{L}}$

## Procedure

1. The apparatus should be accurately leveled by means of screws provided at the base.
2. Connect the water supply to the radial diffuser in the upstream tank.
3. Adjust the level of the discharge pipe by means of the stand and clamp provided to a convenient position.
4. Allow water to flow through the apparatus until all air has been expelled and steady flow conditions are achieved. This can be accomplished by varying the rate of inflow into the apparatus and adjusting the level of the discharge tube.
5. Readings may then be taken from the piezometer tubes and the flow through the apparatus measured.
6. A series of readings can be taken for various through flows.

## Objective

1. To plot the static head, velocity head and total head against the length of the passage in one plain graph paper.
2. To plot the total head loss $h_{L}$, against the inlet kinetic head, $V^{2} / 2 g$, for different inflow conditions in plain graph paper.

## Practice Question

1. What are the assumptions underlying the Bernoulli equation?
2. What is the difference between hydraulic grade line and energy line?

## Experiment No. 2

## BERNOULLI'S THEOREM

## Experimental Data Sheet

| Cross-sectional area of the measuring tank= | Collection time $=$ |  |
| :--- | :--- | :--- |
| Initial point gage reading $=$ | Volume of water $=$ |  |
| Final point gage reading $=$ | Discharge Q | $=$ |


| Piezometer tube no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~A}\left(\mathrm{~cm}^{2}\right)$ | 1.03 | 0.901 | 0.777 | 0.652 | 0.53 | 0.403 | 0.53 | 0.652 | 0.777 | 0.901 | 1.03 |
| $\mathrm{~V}=\mathrm{Q} / \mathrm{A}$ |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{V}^{2} /(2 \mathrm{~g})$ |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{P} / \gamma$ |  |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{H}=\mathrm{P} / \gamma+\mathrm{V}^{2} /(2 \mathrm{~g})$ |  |  |  |  |  |  |  |  |  |  |  |


| Gr. NO. | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $V_{1}{ }^{2} / 2 g$ |  |  |  |  |  |
| $\mathrm{~h}_{\mathrm{L}}$ |  |  |  |  |  |

Signature of the teacher

# Experiment 3 <br> Flow through Venturimeter 



## CE 272: Fluid Mechanics Sessional <br> Experiment No. 3 <br> FLOW THROUGH VENTURIMETER

## General

The converging tube is an efficient device for converting pressure head to velocity head, while the diverging tube converts velocity head to pressure head. The two may be combined to form venturi tube. As there is a definite relation between the pressure difference and the rate of flow. The tube may be made to serve as metering device.

Venturi meter consists of a tube with a constricted throat that produces an increased velocity accompanied by a reduction in pressure followed by a gradual diverging portion in which velocity is transformed back info pressure with slight frictions loss.

## Practical application

The venturimeter is used for measuring the rate of flow of both compressible and incompressible fluids.
The venturimeter provides an accurate means for measuring flow in pipelines. Aside from the installation cost, the only disadvantage of the venturimeter is that it introduces a permanent frictional resistance in the pipelines.


Fig 1. Flow through a venturimeter

## Theory

Consider the Venturimeter shown in Figure 1. Applying the Bernoulli's equation between Point 1 at the inlet and point 2 at the throat, neglecting frictional loss following relation can be obtained.
$\frac{P_{1}}{\gamma}+\frac{V^{2}}{2 g}=\frac{P_{2}}{\gamma}+\frac{V_{2}^{2}}{2 g} \ldots \ldots$. (
Where $P_{1}$ and $V_{1}$ are the pressure and velocity at point $1, P_{2}$ and $V_{2}$ are the corresponding quantities at point $2, \gamma$ is the specific weight of the fluid and g is the acceleration due to gravity from continuity equation, we have.

$$
\begin{equation*}
A_{1} V_{1}=A_{2} V_{2} . \tag{2}
\end{equation*}
$$

Where, $\mathrm{A}_{1}$ and $\mathrm{A}_{1}$ re the cross sectional areas of the inlet and throat respectively since

$$
A_{1}=\frac{\pi}{4} D_{1}^{2}, A_{2}=\frac{\pi}{4} D_{2}^{2}
$$

From Equations (1) and (2), we have

$$
\begin{gather*}
V_{1}=\sqrt{\frac{2 g}{\left(\frac{D_{1}}{D_{2}}\right)^{4}-1} \frac{\left(P_{1}-P_{2}\right)}{\gamma}} \\
=K_{1} H^{1 / 2} \ldots \ldots \ldots \ldots \tag{3}
\end{gather*}
$$

Where,

$$
K_{1}=\sqrt{\frac{2 g}{\left(\frac{D_{1}}{D_{2}}\right)^{4}-1}}
$$

And, $H=\frac{\left(P_{1}-P_{2}\right)}{\gamma}$
The head H is indicated by the piezonmeter tubes connected to the inlet and throat.
The theoretical discharge, $\mathrm{Q}_{\mathrm{t}}$ is given by

$$
\begin{align*}
& Q_{t}=A_{1} V_{1}  \tag{4}\\
& =K H^{1 / 2}
\end{align*}
$$

Where,

$$
\begin{equation*}
K=K_{1} A_{1} \tag{5}
\end{equation*}
$$

## Coefficient of discharge

Theoretical discharge is calculated from theoretical formula neglecting loses, friction losses. For this reason a coefficient is introduced, named coefficient of discharge ( Cd ) which is the ratio of actual discharge to theoretical discharge.
Now, if $C_{d}$ is the coefficient of discharge (also known as the meter coefficient) and $Q_{a}$ is the actual discharge then,

$$
\begin{align*}
C_{d} & =\frac{Q_{a}}{Q_{t}} \\
Q_{a} & =C_{d} Q_{t} \\
& =C_{d} K H^{1 / 2} \\
& =C H^{n} \ldots . . \tag{6}
\end{align*}
$$

The value of Cd may be assumed to be about 0.99 for large meter and about 0.97 or 0.98 for small ones provided the flow is such as to give reasonably high Reynolds number.

## Calibration

One of the objectives of the experiment is to find the values of C and n for a particular meter so that the relation can be used to measure actual discharge only by measuring H .
For five sets of actual discharge and $H$ data we plot $\mathrm{Q}_{\mathrm{a}}$ vs. H in $\log -\log$ paper and draw a best -fit straight line.

The equation of straight line is as follows:
$\log \mathrm{Q}_{\mathrm{a}}=\log \mathrm{CH}^{\mathrm{n}}$
$\log \mathrm{Q}_{\mathrm{a}}=\log \mathrm{C}+\mathrm{n} \log \mathrm{H}$
Now from the plotting, take two points on the straight line say $\left(\mathrm{H}_{1}, \mathrm{Q}_{\mathrm{a} 1}\right)$ and $\left(\mathrm{H}_{2}, \mathrm{Q}_{\mathrm{a} 2}\right)$
From the equation (3), one can get
$\log \mathrm{Q}_{\mathrm{a} 1}=\log \mathrm{C}+\mathrm{n} \log \mathrm{H}_{1}$
$\log \mathrm{Q}_{\mathrm{a} 2}=\log \mathrm{C}+\mathrm{n} \log \mathrm{H}_{2}$
Solving, $n=\frac{\log \frac{Q_{a 1}}{Q_{a 2}}}{\log \frac{H_{1}}{H_{2}}}$
$\mathrm{C}=$ antilog [anti $\log \mathrm{Q}_{\mathrm{a} 1}-\mathrm{n} \log \mathrm{H}_{1}$ ]
So the calibration equation is $\mathrm{Q}_{\mathrm{a}}=\mathrm{CH}^{\mathrm{n}}$
Now $\mathrm{C}=\mathrm{C}_{\mathrm{d}} \mathrm{K}$
$\mathrm{C}_{\mathrm{d}}=\mathrm{C} / \mathrm{K}$
Now from the calibration equation, one can calculate the actual discharge for different H and plot on a plain graph paper. In practice we can use the plot to find actual discharge for any H . Thus the venturi meter is calibrated.

## Objective

1. To find $\mathrm{C}_{\mathrm{d}}$ for the Venturimenter
2. To plot Qa against $H$ in $\log$-log paper and to find (i) exponent of $H$ and(ii) $C_{d}$
3. To calibrate the Venturimeter.

## Practice Questions

1. Why is the diverging angle smaller than the converging angle for a venturimeter?
2. What is cavitation? Discuss its effect on flow through a venturimeter. How can you avoid cavitation in a venturimcter?

Experiment No. 3

## FLOW THROUGH A VENTURIMETER

Experimental Data and Calculation Sheet
Cross sectional area of the measuring tank, $\mathrm{A}=$

| Pipe diameter, | $\mathrm{D}_{1}=\square$ | Area of the pipe, $\quad \mathrm{A}_{1}=\square$ |
| :--- | :--- | :--- |
| Throat diameter | $\mathrm{D}_{2}=\square$ | Area of the throat, $\quad \mathrm{A}_{2}=\square$ |
| Temperature of water, $\mathrm{t}=\square$ | Kinematic viscosity of water $\mathrm{v}=\square$ |  |
| Initial point gage reading $=\square$ | Final point gage reading $=\square$ |  |


| No. |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| of <br> obs. | Volume <br> of water <br> v | Time <br> T | Actual <br> Discharge <br> $\mathrm{Q}_{\mathrm{a}}$ | Piezometer reading <br> $\mathrm{h}_{1}$ |  | Left <br> $\mathrm{h}_{1}$ | Right <br> $\mathrm{h}_{2}$ | Diff. <br> H | $\mathrm{k}_{1}$ | k | Theoretical <br> discharge <br> $\mathrm{Q}_{\mathrm{t}}$ | $C_{d}=\frac{Q_{a}}{Q_{t}}$ | | $V_{2}=\frac{Q_{a}}{A_{2}}$ |
| :---: | | Reynolds <br> number <br> $\mathrm{R}_{\mathrm{e}}$ |
| :---: |


| Group No. |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Actual discharge Qa |  |  |  |  |  |
| Head difference H |  |  |  |  |  |
| Coefficient of discharge |  |  |  |  |  |
| Reynolds number |  |  |  |  |  |

## Experiment 4

 Flow through an Orifice

## CE 272: Fluid Mechanics Sessional Experiment No. 4 FLOW THROUGH AN ORIFICE

## General

An orifice is an opening in the wall of a tank or in a plate normal to the axis of a pipe, the plate being either at the end of pipe or in some intermediate location. An orifice is characterized by the fact that the thickness of the wall or plate is very small relative to the size of the opening. For a standard orifice there is only a line contact with fluid.


Fig 1. Jet Contraction
Where the streamlines converge in approaching an orifice, they continue to converge beyond the upstream section of the orifice until they reach the section xy where they become parallel. Commonly this section is about $0.5 D_{0}$ from the upstream edge of the opening, where $\mathrm{D}_{\mathrm{o}}$ is diameter of the orifice. The section $x y$ is then a section of minimum area and is called the vena contracta. Beyond the vena contracta the streamlines commonly diverge because of frictional effects.

## Practical application

The usual purpose of an orifice is the measurement or control of flow from a reservoir. The orifice is frequently encountered in engineering practice operating under a static head where it is usually not used for metering but rather as a special feature in a hydraulic design. Another problem of orifice flow, which frequently arises in engineering practice, is that of discharge from an orifice under falling head, a problem of unsteady flow.

## Coefficient of contraction:

The ratio of the area of a jet at the vena contracta to the area of the orifice is called the coefficient of contraction.

## Coefficient of velocity:

The velocity that would be attained in the jet if the friction did not exist may be termed the theoretical velocity. The ratio of actual to the theoretical velocity is called coefficient of velocity.

## Coefficient of discharge:

The ratio of the actual rate of discharge Qa to the theoretical rate of discharge Q (the flow that would occur if there were no friction and no contraction) is defined as the coefficient of discharge.

Consider a small orifice having a cross-sectional area A and discharging water under a constant head h as shown in the figure below. Applying Bernoulli's theorem between the water surface and point 0 .

$$
\begin{aligned}
& H=0+v^{2} / 2 g \\
& \text { so, } V_{t}=\sqrt{2 g H}
\end{aligned}
$$

where g is the acceleration due to gravity. Let Qa be the actual discharge.
So theoretical discharge Qt is given by
$Q_{1}=A \sqrt{2 g H}$
Then the coefficient of discharge, Cd is given by
$C_{d}=\frac{Q_{a}}{Q_{t}}$


Fig 2. Co-efficient of Velocity by Co-ordinate Method

Let H be the total head causing flow and section- $\mathrm{c}-\mathrm{c}$ represents the vena contract as shown in the figure. The jet of water has a horizontal velocity but is acted upon by gravity with a downward acceleration of g . Let us consider a particle of water in the jet at P and let the time taken for this to move particle from O to P be t .
Let x and y be the horizontal and vertical co-ordinates of P from O , respectively. Then, $x=V_{a} t$
and
$y=\frac{1}{2} g t^{2}$
Equating the value of $t^{2}$ from these two equations, one obtains
$\frac{x^{2}}{V_{a}^{2}}=\frac{2 y}{g}$
$V a=\sqrt{\frac{g x^{2}}{2 y}}$
But, the theoretical velocity, $V_{t}=\sqrt{2 g H}$
Hence, the coefficient of velocity, Cv is given by

$$
C_{v}=\frac{v_{a}}{v_{t}}=\sqrt{\frac{x^{2}}{4 y H}}
$$

And the head loss is given by
$H_{l}=\left(1-C_{v}{ }^{2}\right) H$
$C_{v}=\frac{v_{a}}{v_{t}}=\frac{v_{a}}{\sqrt{2 g H}}$
Coefficient of contraction, Cc is defined as the area of jet at vena contracta to the area of orifice, thus,
$C_{c}=\frac{A_{a}}{A}$
It follows that
$C_{d}=C_{c} x C_{v}$

## Description of the orifice meter:

The P6228 Orifice Flowmeter consists of a 22 mm bore acrylic tube with a interchangeable sharp edge orifice plate of 8 mm . The downstream bore of the orifice is chamfered at 40 degree angle to provide an effective orifice plate thickness of 0.35 mm . The flanges of orifice meter have been especially designed to incorporate corner tappings immediately adjacent to orifice plate by the use of piezometer rings machined directly into the face of the flanges. The flanges also incorporate D and $\mathrm{D} / 2$ tappings. The design of the orifice plates conform with the British Standard for flow measurement BS1042.

The orifice plate assembly is shown in Figure 2


Fig 3. P6228 Orifice Plate Meter

## Theory:

Due to the sharpness of contraction in flow area at the orifice plate a vena contracta is formed. Applying the continuity equation between the upstream conditions at section 1 and the vena contracta:

$$
\mathrm{Q}=\mathrm{A}_{1} \mathrm{~V}_{1}=\mathrm{A}_{\mathrm{c}} \mathrm{~V}_{\mathrm{c}}
$$

Where suffix c denotes the vena contracta
Applying Bernoulli's equation, neglecting losses and assuming a horizontal installation:
$\frac{P_{1}}{\rho g}+\frac{V_{1}^{2}}{2 g}=\frac{P_{c}}{\rho g}+\frac{V_{c}{ }^{2}}{2 g}$
Rearranging
$\frac{P_{1}-P_{c}}{\rho g}=H=\frac{V_{c}^{2}-V_{1}^{2}}{2 g}$
And solving for Vc


Fig 4. Orifice Plate Meter

$$
V_{c}=\sqrt{\frac{2\left(\mathrm{P}_{1}-\mathrm{P}_{\mathrm{c}}\right)}{\rho\left[1-\frac{V_{1}^{2}}{V_{c}^{2}}\right]}}
$$

The flow area at the vena contracta is not known and therefore a coefficient of contraction may be introduced so that $\mathrm{Cc}=\mathrm{Ac} / \mathrm{A} 2$
$Q=A_{c} V_{c}$
The coefficient of contraction will be included in the coefficient of discharge and the equations rewritten in terms of the orifice area A2 with any uncertainties and errors eliminated by the experimental determination of the coefficient of discharge. The volumetric flow rate is then given by
$Q=C_{d} A_{2} \sqrt{\frac{2\left(\mathrm{P}_{1}-\mathrm{P}_{2}\right)}{\rho\left[1-\frac{V_{1}^{2}}{V_{2}^{2}}\right]}}=C_{d} A_{2} \sqrt{\frac{2 g H}{1-\beta^{4}}}$
Here,
$\beta=\sqrt{\frac{V_{1}}{V_{2}}}=\sqrt{\frac{A_{2}}{A_{1}}} ; H=\frac{\left(P_{1}-P_{2}\right)}{\gamma}$
The position of the manometer tappings has a small effect on the values of the discharge coefficients which also vary with the area ratio, with pipe size and with Reynolds number.

## Apparatus:

1. Constant head water tank
2. Orifice
3. Discharge measuring tank
4. Stop watch
5. Point gauge

## Procedure:

## Co-efficient of Velocity by Co-ordinate Method

1. Measure the diameter of the orifice.
2. Supply water to the tank.
3. When the head at the tank (measured by a manometer attached to the tank) is steady record the reading of the manometer.
4. Measure the x and y co-ordinate of the jet from the vena contracta.
5. Measure the flow rate.
6. Repeat the procedure for different combinations of discharge.

## Orifice Plate Meter

1. Start the pump and establish a water flow through the test section. Raise the swivel tube of the outlet tank so that it is close to the vertical. Adjust the vent regulating valve to provide a small overflow from the inlet tank and overflow pipe. Ensure that any air bubbles are bled from the manometer.
2. Set up a series a of flow conditions with differential heads. At each condition carefully measure the flow rate using the volumetric tank and a stop watch. Record the differential head across the orifice plate twice, i.e. for the D and $\mathrm{D} / 2$ tappings.
3. Determine the theoretical discharge, actual discharge and the coefficient of discharge.
4. Plot Actual discharge vs. pressure head difference on $\log -\log$ graph paper.
5. Develop the Calibration equation and draw the calibration graph.

## Objective

1. To find the value of $\mathrm{C}_{\mathrm{d}}$ for the orifice.
2. To plot $\mathrm{Q}_{\mathrm{a}}$ vs. H in $\log -\log$ paper and to find the value of (a) the exponent of H and (b) $\mathrm{C}_{\mathrm{d}}$.
3. To find $\mathrm{C}_{\mathrm{v}}$ for the orifice.
4. To find the head loss, $\mathrm{H}_{\mathrm{L}}$.
5. To plot $\mathrm{V}_{\mathrm{a}}$ vs. H in $\log -\log$ paper and to find (a) $\mathrm{C}_{\mathrm{v}}$ and (b) the exponent of H .

## Practice Questions

1. What is an Orifice? What is the purpose of orifice?
2. What is vena contraacta?
3. What are the coefficient of velocity, coefficient of contraction and coefficient of discharge for an orifice? On what factors do these coefficients depend?

Experiment No. 4
FLOW THROUGH AN ORIFICE
Observation and Calculation Sheet

Area of the orifice $=$
Area of the pipe $=$

| Quantity of Water Collected Q litre | Time to <br> Collect <br> Water, t <br> sec | Volumetric <br> Flow Rate, Q <br> litres/min | D Tappings <br> Upstream $\mathrm{H}_{1}$ (m) | D/2 Tappings <br> Downstream <br> $\mathrm{H}_{2}$ (m | D \& D/2 <br> Tappings <br> Diff. Head <br> H (m) | $\mathrm{C}_{\mathrm{d}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
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Co-efficient of Velocity by Co-ordinate Method
Observation and Calculation Sheet

| No <br> Of <br> Obs. | Horizontal <br> Coordinate <br> x | vertical <br> Coordinate <br> y | Actual <br> velocity <br> $\mathrm{V}_{\mathrm{a}}$ | Coeff. <br> of <br> velocity <br> $\mathrm{C}_{\mathrm{v}}$ | Head <br> loss <br> $\mathrm{H}_{\mathrm{L}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |


| No of observation |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Actual discharge, $\mathrm{Q}_{\mathrm{a}}$ |  |  |  |  |  |
| Theoretical Discharge $\mathrm{Q}_{\mathrm{t}}$ |  |  |  |  |  |
| Actual Velocity $\mathrm{V}_{\mathrm{a}}$ |  |  |  |  |  |
| Theoretical velocity $\mathrm{V}_{\mathrm{t}}$ |  |  |  |  |  |
| Actual head H |  |  |  |  |  |

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# Experiment 5 <br> Flow through an External Cylindrical Mouthpiece 



## CE 272: Fluid Mechanics Sessional Experiment No. 5

## FLOW THROUGH AN EXTERNAL CYLINDRICAL MOUTHPIECE

## General

If a small tube is attached to an orifice, it is called mouthpiece. The standard length of a mouthpiece is 3 d , where d is the diameter of the orifice. If the length is less than 3d, jet after passing the vena contracta does not occupy the tube fully and thus acts as orifice. If the length is greater than 3d, it acts as pipe.

The effect of adding a mouthpiece to an orifice is to increase the discharge. The pressure at vena contracta is less than atmospheric, so a mouthpiece decreases the pressure at vena contracta and increases the effective head causing the flow, hence, discharge is increased. The pressure at outlet is atmospheric but as the velocity of the vena contracta is greater than the velocity at outlet, the pressure at vena contracta will be less than atmospheric.

## Practical application

Flow through an orifice can not represent the flow through a pipe properly. Also in orifice, coefficient of discharge is only 0.62 . So to increase discharge from a reservoir and represent the flow through pipe mouthpiece is used.


Fig 1. Flow Through an External Cylindrical Mouthpiece

## Theory

Consider an external cylindrical mouthpiece of area A discharging water under a constant head H as shown in the figure. Applying Bernoulli's equation at point 1 and 3,
$H=\frac{V^{2}}{2 g}$
$V=\sqrt{2 g H}$
Then the theoretical discharge, $\mathrm{Q}_{\mathrm{t}}$, is given by
$Q_{1}=A \sqrt{2 g H}$
where A is the area of the mouthpiece. Let $\mathrm{Q}_{\mathrm{a}}$ be the actual discharge then the coefficient of discharge $\mathrm{C}_{\mathrm{d}}$ is given by,
$C_{d}=\frac{Q_{a}}{Q_{t}}$

## Apparatus

1. Constant head water tank
2. Mouth piece
3. Discharge measuring tank
4. Stop watch
5. Point gauge

## Procedure

1. Measure the diameter of the orifice.
2. Attach the mouth piece to the orifice of the constant head water tank.
3. Supply water to the tank.
4. When the head at the tank (measured by a manometer attached to the tank) is steady, record the reading of the manometer.
5. Measure the flow rate.
6. Repeat the procedure for different combinations of discharge.

## Objective

1. To find $\mathrm{C}_{\mathrm{d}}$ for the mouthpiece.
2. To plot $Q_{a}$ vs. $H$ in $\log -\log$ paper, and to find (a) $C_{d}$ and (b) the exponent of $H$

## Practice Questions

1. Explain why the discharge through an orifice is increased by fitting a standard short tube to it.
2. What will happen to the coefficient of discharge if the tube is shorter than the standard length or the head causing the flow is relatively high?

Experiment 5
FLOW THROUGH AN EXTERNAL CYLINDRICAL MOUTHPIECE

## Calculation Sheet

Diameter of the mouthpiece, $\mathrm{D}=$
Area of the mouthpiece, $\mathrm{A}=$
Cross-sectional area of the measuring tank= $\qquad$
Head correction, $\mathrm{h}^{\prime}=$
Initial point gauge reading=
Final point gauge reading=
$\qquad$
Difference in gauge reading= $\qquad$
Observed head, $\mathrm{h}=$

| No. of <br> Obs | Actual <br> head <br> $\mathrm{H}=\mathrm{h}-\mathrm{h}^{\prime}$ | Volume <br> of <br> water | Collection <br> time <br> T | Actual <br> Discharge <br> $\mathrm{Q}_{\mathrm{a}}$ | Theoretical <br> Discharge <br> $\mathrm{Q}_{\mathrm{t}}$ | Co-efficient. <br> of <br> Discharge <br> $\mathrm{C}_{\mathrm{d}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |


| No of observations |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Actual discharge, Qa |  |  |  |  |  |
| Actual Head H |  |  |  |  |  |

## Experiment 6

Flow over a sharp crested rectangular weir


## CE 272: Fluid Mechanics Sessional <br> Experiment No. 6 FLOW OVER A SHARP-CRESTED RECTANGULAR WEIR

## General

A weir is an overflow structure built across an open channel for the purpose of measuring the flow. Weirs are commonly used to measure flow of water, but their use in measurement of other liquids is increasing.

Classified with reference to the shape of the opening through which the liquid flows, weirs may be rectangular, triangular, trapezoidal, circular, parabolic or of any other regular form. The first three forms are most commonly used for measurement of water. Classified with reference to the form of crest (the edge or the top surface with which liquid comes in contact) weirs may be sharp-crested or broad-crested.
The sharp-crested rectangular weir has a sharp upstream edge so formed that the liquid in passing touches only a line.

The overfalling stream is termed as 'nappe'. The nappe of a sharp crested weir as shown in fig is contracted at its underside by the action of the vertical components of the velocity just upstream from the weir. This is called crest contraction. If the sides of the opening also have sharp upstream edge so that the nappe is contracted in width, the weir is said to have end contractions and is usually called a contracted weir.


Fig 1. Path lines of flow over rectangular sharp crested weir

## Practical application

Shallow rivers are often made navigable by building, dams across the river at certain sections over which the water may flow. During a drought little or no water will flow past the dam, but after heavy rains the water flows over the dam, thus converting it into a weir. Also flow through canal is measured by weirs.

## Theory

The relationship between discharge and head over the weir can be developed by making the following assumptions as to the flow behavior:

1. Upstream of the weir, the flow is uniform and the pressure varies with depth according to the hydrostatic equation $\mathrm{P}=\gamma \mathrm{h}$.
2. The free surface remains horizontal as far as the plane of the weir, and all particles passing over the weir move horizontally. (In fact, the free surface drops as it approaches the weir).
3. The pressure throughout the sheet of liquid or nappe, which passes over the crest of the weir, is atmospheric.
4. The effects of viscosity and surface tension are negligible.
5. The upstream approach velocity head is neglected.


Fig 2. Flow Over a Sharp-Crested weir

Now consider the sharp-crested weir in the figure. Let H be the working head and B is the length of the weir.

Let us consider a small horizontal string of thickness dh under a head $h$. The strip can be considered as an orifice.

Therefore, the theoretical discharge through the strip
$\mathrm{dQ}_{1}=$ area of the strip x velocity
$=(B d h) \sqrt{2 g h}$
Integrating between the limits 0 and H , the total theoretical discharge over the weir is given by
$Q_{t}=\frac{2}{3} \sqrt{2 g} \mathrm{BH}^{3 / 2}$
Let $\mathrm{Q}_{\mathrm{a}}$ be the actual discharge. Then the co-efficient of discharge, $\mathrm{C}_{\mathrm{d}}$, is given by $C_{d}=\frac{Q_{a}}{Q_{t}}$
Therefore,
$Q_{a}=\frac{2}{3} C_{d} \sqrt{2 g} \mathrm{BH}^{3 / 2}$
$=K C_{d} H^{3 / 2}$
where,
$K=\frac{2}{3} \sqrt{2 g}$ B
For a contracted weir, B is equation (5) should be replaced by effective length ( $B^{\prime}$ ) which is given by
$B^{\prime}=B-0.1 n H$
Where n is the number of end contraction.


Fig 3. Weir with end contractions

## Apparatus

1. A constant steady water supply with a means of varying the flow rate.
2. An approach channel
3. A rectangular weir plate
4. A flow rate measuring facility
5. A point gauge for measuring H

## Procedure

1. Measure the height and length of the weir. Position the weir plate at end side of the approach channel, in a vertical plane, with sharp edge on the upstream side.
2. Allow water to the channel so that water flows over the weir and wait until water surface comes to a steady condition.
3. Ventilate the nappe with a pipe.
4. Set an elevation of zero of the point gauge with reference to the bottom of the channel.
5. Check again whether the nappe is ventilated or not. If not, ventilate it.
6. Carefully set the point gauge on the water surface 4 to 6 ft upstream of the weir and take the gauge reading. The water surface may be slightly fluctuating.
7. Take the discharge reading from the flow meter.

## Objective

1. Observation of the nappe for ventilated and non-ventilated conditions.
2. To find $\mathrm{C}_{\mathrm{d}}$ for the weir
3. To plot $\mathrm{Q}_{\mathrm{a}}$ vs. H in a plain graph paper.
4. To plot $\mathrm{Q}_{\mathrm{a}}$ vs. H in a log-log graph paper and to find (1) the exponent of H and (2) Cd

## Practice Questions

1. What are the assumptions made in deriving this equation?
2. Discuss the effects of lateral contraction, in case of contracted weir, on the flow over the weir.

## Experiment No. 6 <br> FLOW OVER A SHARP-CRESTED WEIR <br> Experimental Data Sheet

Width of the weir, $\mathrm{B}=$
Height of the weir, $\mathrm{P}=$
Initial point gage reading $=$
Final point gage reading $=$

| No <br> of <br> Obs. | Actual <br> discharge <br> $\mathrm{Q}_{\mathrm{a}}$ | Ventilated Condition |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Head <br> H | Theoretical <br> discharge <br> $\mathrm{Q}_{\mathrm{t}}$ | Co-efficient. of <br> discharge <br> $\mathrm{C}_{\mathrm{d}}$ |
|  |  |  |  |  |
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## Experiment 7 <br> Flow over a V-notch



## CE 272: Fluid Mechanics Sessional <br> Experiment. No. 7 <br> FLOW OVER A V-NOTCH

## General

The most common types of sharp-crested weir are the rectangular weir and the triangular weir. The triangular weir or V-notch is preferable to the rectangular weir for the measurement of wide range of flow.

## Practical application

When small quantity of flow need to be measured the V-notch weir is preferable because the triangular cross-section of the flow 'nappe' leads to a relatively greater variation in head. Vnotch weir has the advantage that it can function for a very small flows and also measure reasonably larger flows as well.


Fig 1. Flow over a V-Notch

## Theory

Consider the V-notch shown in the figure. Let H be the height of water surface and $\theta$ be the angle of notch. Then width of the notch at the water surface.
$L=2 H \tan \frac{\theta}{2}$
Consider a horizontal strip of the notch of thickness dh under a head h . Then, width of the strip, $W=2(H-h) \tan \frac{\theta}{2}$

Hence, the theoretical discharge through the strip
$d Q_{t}=$ area of the strip x velocity $=2(\mathrm{H}-\mathrm{h}) \tan \frac{\theta}{2} d h \sqrt{2 g h}$
Integrating between the limits 0 and H and simplifying, the total theoretical discharge over the notch is given by

$$
\begin{align*}
Q_{t} & =\frac{8}{15} \sqrt{2 g} \tan \frac{\theta}{2} H^{5 / 2}  \tag{4}\\
& =K H^{5 / 2} \ldots \ldots \ldots \ldots \ldots \tag{5}
\end{align*}
$$

Where,
$K=\frac{8}{15} \sqrt{2 g} \tan \frac{\theta}{2}$.
Let $Q_{a}$ be the actual discharge, Then the confficient of discharge, Cd is given by
$C_{d}=\frac{Q_{a}}{Q_{t}}$
$Q_{a}=K C_{d} H^{5 / 2}$
The co-efficient of discharge depends on relative head $(\mathrm{H} / \mathrm{P})$, relative height $(\mathrm{P} / \mathrm{B})$ and angle of the notch $(\theta)$

From hydraulic point of view a weir may be fully contracted at low heads while at increasing head it becomes partially contracted. The flow regime in a weir is said to be partially contracted when the contractions along the sides of the V-notch are not fully developed due to proximity of the walls and bed of approach channel. Whereas a weir which has an approach channel and whose bed and sides of the notch are sufficiently remote from the edges of the V-notch to allow for a sufficiently great approach velocity component parallel to the weir face so that the contraction is fully developed is a fully contracted weir. In case of a fully contracted weir $\mathrm{C}_{\mathrm{d}}$ is fairly constant for a particular angle of notch.
At lower heads, frictional effects reduce coefficients. For the most common angle of notch 90 degree, the discharge coefficient, $\mathrm{C}_{\mathrm{d}}$ is about 0.6.

## Apparatus

1. A constant steady water supply with a means of varying the flow rate.
2. An approach channel
3. A V-notch weir plate
4. A flow rate measuring facility
5. A point gauge for measuring H .

## Procedure

1. Position the weir plate at the end of approach channel, in a vertical plane, with the sharp edge on the upstream side.
2. Admit water to channel until the water discharges over the weir plate.
3. Close the flow control valve and allow water to stop flowing over weir.
4. Set the point gauge to a datum reading.
5. Position the gauge about half way between the notch plate and stilling baffle.
6. Admit water to the channel and adjust flow control valve to obtain heads, H , increasing in steps of 1 cm .
7. For each flow rate, stabilize conditions, measure and record H .
8. Take readings of volume and time using the volumetric tank to determine the flow rate.

## Objective

1. To find Cd for the V-notch.
2. To plot Qt vs. Qa in a plain graph paper.
3. To plot $Q_{a}$ vs. $H$ in a log-log paper and to find (a) the exponent of $H$ and (b) $C_{d}$

## Practice Questions

1. Why does the V -notch give more accurate flow measurement than any other weirs and orifices when the flow is fluctuating?
2. What is the average value of $\mathrm{C}_{\mathrm{d}}$ for a $90^{\circ} \mathrm{V}$-notch? Does it depend on flow condition (partially or fully contracted)?

Experiment No. 7
FLOW OVER A V-NOTCH
Observation and Calculation Sheet
Angle of the notch, $\theta=$
$\mathrm{K}=$
Cross-sectional area of the measuring tank =
Initial point gauge reading =
Final point gauge reading =

| No. of <br> Obs. | Vol. <br> of <br> water | Collection <br> time <br> T | Actual <br> discharge <br> $\mathrm{Q}_{\mathrm{a}}$ | Effective <br> head <br> H | Theoretical <br> discharge <br> $\mathrm{Q}_{\mathrm{t}}$ | Co-eff. <br> of <br> discharge |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |


| No of <br> observation |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Actual <br> discharge $\mathrm{Q}_{\mathrm{a}}$ |  |  |  |  |  |
| Effective <br> head H |  |  |  |  |  |
| Theoretical <br> discharge |  |  |  |  |  |

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## Experiment 8 <br> Fluid Friction in a pipe



## CE 272, Fluid Mechanics Sessional Experiment No. 8 FLUID FRICTION IN A PIPE

## General

Head loss in a pipe flow is mainly due to friction in pipes and again friction is due to roughness of pipes. It has been proved that friction is dependent not only upon the size and shape of the projection of roughness, but also upon their distribution or spacing.

## Practical application

Flow through a single pipe line, pipes in series and parallel and also in pipe network system, cause head loss due to friction. The head loss from source to the point of interest due to the friction along the pipe also provides the basis of pipe size (diameter) design. This experiment gives an estimate of head loss due to friction in the pipe per unit length of the pipe.

## Theory

Friction loss is the loss of energy or head that occurs in the pipe flow due to viscous effects generated by the surface of the pipe. This energy loss is dependent on the wall shear stress between the fluid and pipe surface, and the shear stress of a flow dependent on whether the flow is turbulent of laminar. For turbulent flow, the pressure drop is dependent on the roughness of the surface while in laminar flow the roughness effects of the wall are negligible. This is due to fact that for turbulent flow a thin viscous layer is formed near the pipe surface which causes loss of energy while in laminar flow this viscous layer is nonexistent.

Friction loss has several causes:

- Condition of flow
- Movement of fluid molecules against each other
- Movement of fluid molecules against inside surface of pipe

If the head loss in a given length of uniform pipe is measured at different values of the velocity, it will be found that, as long as the velocity is low enough to secure laminar flow. the head loss, due to friction, will be directly proportional to the velocity. But with increasing velocity, at some point where the visual observation in a transparent tube would show that the flow changes from laminar to turbulent, there will be an abrupt increase in the rate at which the head loss varies. If the logarithms of those two variables are plotted on linear scales or if the values are plotted directly on log-log paper, it will be found that, after a certain transition region has been passed, lines will be obtained with slopes ranging from about 1.75 to 2.00 .


Fig 1. Head loss due to Friction in a pipe

It is thus understood that for laminar flow the drop in energy due to friction varies as V , while for turbulent flow the friction varies as $\mathrm{V}^{\mathrm{n}}$, where n ranges from about 1.75 to 2.00. The lower value of 1.75 for turbulent flow is found for pipes with very smooth walls; as the wall roughness increases, the value of $n$ increases up to its maximum value of 2.00.

However, velocity is not the only factor that determines whether the flow is laminar or turbulent. The criterion is Reynolds number. For a circular pipe the significant linear dimension L is usually taken as the diameter D , and thus
$R_{e}=\frac{V D}{v}$
For circular pipe when,
$\begin{array}{ll}\mathrm{R}_{\mathrm{e}}<2000 & \text { Flow is Laminar } \\ 2000<\mathrm{R}_{\mathrm{e}}<4000 & \text { Flow is Transitional } \\ \mathrm{R}_{\mathrm{e}}>4000 & \text { Flow is Turbulent }\end{array}$
Head loss, $\mathrm{h}_{\mathrm{L}}$ can be generalized as proportional with the exponential power of velocity, V by
$h_{L} \propto V^{n}$
where n is the exponent of velocity
Therefore, $h_{L}=K V^{n}$
where K is a constant.

Early experiment on the flow of water in long, straight, uniform circular pipes indicated that head loss varied directly with velocity head and pipe length and inversely with pipe dia. Darcy Weisbach proposed the formula for the turbulent flow,
$h_{L}=4 f \frac{L}{D} \frac{V^{2}}{2 g} \quad$ or, $\quad f=\frac{D}{4 L} \frac{2 g}{V^{2}} h_{L}$

Where, $\mathrm{f}=$ friction factor
For laminar flow head loss $\left(\mathrm{h}_{\mathrm{L}}\right)$ given by Hagen-Poiseuille is
$h_{L}=\frac{32 \mu L V}{\rho g D^{2}}$
For laminar flow The striking feature of the equation is that it involves no empirical coefficient or experimental factors of any kind, except for the physical properties of fluid such as, viscosity, and density.
$f=\frac{64}{R_{e}}$ (for circular pipe)
Therefore, friction factor (f) can be related empirically as
$f=\varphi\left(R_{e}\right)$
$=C R_{e}{ }^{m}$
Where m is the exponent of Reynolds number and C is a constant.
From this it would appear that in laminar flow the friction is independent of the roughness of the pipe wall.

## Apparatus

1. Pipe friction apparatus
2. Stop watch
3. Discharge measuring facility
4. Thermometer.

## Procedure

1. Measure the diameter of the pipe and distance between the two tapings.
2. Prime the mercury manometer.
3. Connect the test section pipe to the main water supply pipe.
4. Open flow control valve, priming test section and pipe work.
5. Open clips on water manometer, allowing water to circulate through the system until all the air is expelled.
6. Close pipe clips.
7. Bleed mercury manometer via bleed screws in conjunction with the control valves.
8. Close flow control valve.
9. Observe datum level on manometer.
10. To achieve maximum flow fully open flow control valve. Note levels in manometer and measure flow rate. Repeat for different control valve position.
11. When the mercury level is below 35 mm , open pipe clips near water manometer and take readings on both manometers, The level in the water manometer can be adjusted by operating the air valve or the hand pump.
12. For low flows the constant head tank should be used as follows. Close control valve, close supply valve, disconnect inlet pipe from the bench and connect to constant head tank. Connect tank inlet to bench supply. Carefully open bench valve, fill head tank and adjust until water discharges from outlet pipe with flow control valve open. Take readings as before and measure flow rate. Measure the water temperature.

## Objective

1. To find the frictional loss
2. To plot $h_{L}$ vs velocity in log-log paper and determine the empirical relationship of the form $h_{L}=K V^{n}$.
3. To plot $f$ vs. $R_{e}$ in a log-log paper and find the empirical relation of the form $f=$ $\mathrm{CR}_{\mathrm{e}}{ }^{\mathrm{m}}$
4. To plot $h_{L}$ vs velocity for turbulent flow condition and obtain an average value of $f$.

## Practice Questions

1. What are the factors upon which the frictional loss in a pipe depends?
2. Discuss the relation between fluid fricyion and velocity of a pipe for different flow condition?

Experiment No. 8

## FLUID FRICTION IN A PIPE

Calculation and Data Sheet
Diameter of the pipe, $\mathrm{D}=$
Area of the pipe, $\mathrm{A}=$
Temperature of water, $\mathrm{t}=$
$\rho=\quad, \mu \quad=\quad, v=$

| No <br> of <br> obs | Volume <br> $\mathrm{V}_{1}$ | Time <br> T | Discharge <br> Q | Velocity <br> V | Reynolds <br> No <br> $\mathrm{R}_{\mathrm{e}}$ | $\mathrm{h}_{\mathrm{L}}$ <br> $\mathrm{m}_{2} \mathrm{of}$ <br> $\mathrm{H}_{2} \mathrm{O}$ | f |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |


| No. of <br> observation |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Discharge Q |  |  |  |  |  |
| Velocity V |  |  |  |  |  |
| Reynolds No. $\mathrm{R}_{\mathrm{e}}$ |  |  |  |  |  |
| $\mathrm{h}_{\mathrm{L}}\left(\mathrm{m} \mathrm{of}_{\mathrm{H}} \mathrm{O}\right)$ |  |  |  |  |  |
| f |  |  |  |  |  |

Signature of the Teacher

## Experiment 9 Head Loss due to Pipe Fittings



## CE 272: Fluid Mechanics Sessional Experiment No. 9 <br> HEAD LOSS DUE TO PIPE FITTINGS

## General

In practical setting, fluid flows through different pipe fittings such as sudden contraction, sudden enlargement valve, elbow or bend, tee section etc. Sudden changes in the flow path result in secondary flow patterns, denoted as separation region and vena contracta (flow area contraction due to secondary flow). Vortices and eddies occur in these regions, consuming energy and resulting in an observable pressure drop. Large pressure drops are observed as the fluid is forced through non-streamlined passages. These losses through valves and fittings are known as minor losses or fitting losses. Due to separation of flow, the fluid energy reduces in the downstream of the component than the upstream.
Frictional losses are avoided here since the lengths of pressure measuring points (tapping points) are comparatively small.

## Practical application

In any pipe network there may sudden change in pipe diameter, In any change in pipe diameter there is considerable head loss and we need to calculate the loss. From this experiment, we can determine the coefficient to calculate the losses.

## Theory

## Loss Due to sudden contraction

The loss of head in a sudden contraction is not only due to the contraction itself but also due to sudden expansion which follows the contraction as shown in figure.
Head loss in sudden contraction $\mathrm{H}_{\mathrm{LC}}=\left(\frac{p_{1}}{\gamma}-\frac{p_{2}}{\gamma}\right)+\left(\frac{V^{2}{ }_{2}}{2 g}-\frac{V_{1}^{2}}{2 g}\right)$

$$
\begin{aligned}
& =H_{1}-\left(\frac{V_{2}^{2}}{2 g}-\frac{V_{1}^{2}}{2 g}\right) \\
H_{L C} & =K_{C} \frac{v_{2}^{2}}{2 g}=k_{1} v_{2}^{n}
\end{aligned}
$$



Fig 1. Sudden Contraction

## Loss due to sudden expansion

The loss of head in a sudden contraction is due to the formation of eddies at the corner as shown in Figure.

Head loss in a sudden expansion $H_{L E}=\left(\frac{V_{2}^{2}}{2 g}-\frac{V_{1}^{2}}{2 g}\right)-\left(\frac{P_{3}}{\gamma}-\frac{P_{2}}{\gamma}\right)$

$$
=\left(\frac{V_{2}^{2}}{2 g}-\frac{V_{1}^{2}}{2 g}\right)-H_{2}
$$

$$
H_{L E}=K_{E} \frac{\left(v_{2}-v_{1}\right)^{2}}{2 g}=K_{2}\left(V_{2}-V_{1}\right)^{n}
$$



Fig 2. Sudden Expansion

## Experimental Setup



Fig 3. Sudden Contraction and Expansion


Fig 4. 10mm pipe with Four Elbows

## Apparatus

1. Fluid friction apparatus
2. Stop watch
3. Discharge measuring facility
4. Thermometer

## Procedure

## Sudden Expansion and Contraction of Pipe

1. Measure the diameter of the pipes.
2. Prime the mercury manometer
3. Connect the test section pipe to the main water supply pipe
4. Open flow control valve, priming test section and pipe work.
5. Open clips on water manometer, allowing water to circulate through the system until all the air is expelled.
6. Close pipe clips.
7. Bleed mercury manometers via bleed sewers in conjunction with control valves
8. Close flow control valve.
9. Observe datum level on manometers.
10. To achieve maximum flow fully open flow control valve. Note levels in manometer and measure flow rate. Repeat for different control valve position.
11. When the mercury level is below 35 mm open pipe clipps near water manometer and take readings on both manometers. The level in the water manometer can be adjusted by operating the air valve or the hand pump.
12. For low flows the constant head tank should be used as follows. Close control valve, close supply valve, disconnect inlet pipe from the bench and connect to constant head tank. Connect tank inlet to bench supply. Carefully open bench valve, fill head tank and adjust until water discharges from outlet pipe with flow control valve open. Take readings as before and measure flow rate. Measure the water temperature.

## Loss due to Elbows

1. Connect the test section pipe with four elbows to the main water supply pipe
2. Measure the pressure head at upstream and downstream of the elbow sections.
3. Calculate the pressure head difference. This loss is due to both friction and elbows.
4. Calculate the actual discharge and Reynolds number
5. To measure the loss due to friction in a straight pipe of equal length, find the friction factor (f) from the Stanton Diagram figure 5 using relative roughness $(\varepsilon / D)$ and Reynolds number (Re)
6. Find the loss due to friction using the Darcy Weichbach formula (for turbulent flow)
7. Determine the minor loss due to elbows.

## Objective

1. To determine the minor loss
2. To plot $\mathrm{H}_{\mathrm{LC}}$ vs. $\mathrm{V}_{2}$ in log-log paper and determine the exponent n and coefficient $\mathrm{k}_{\mathrm{t}}$
3. To plot $\mathrm{H}_{\mathrm{LE}}$ vs $\left(\mathrm{V}_{2}-\mathrm{V}_{1}\right)$ in $\log$-log paper and determine the exponent n and coefficient $\mathrm{k}_{2}$.

## Practice Questions

1. For the same diameter ratios and the same velocities the loss due to sudden expansion is greater than the loss due to a corresponding contraction. Explain why?
2. Write down the different types of losses that may occur in pipe flow.
3. What are the type of fittings used in a pipe?

Relative Roughness $\epsilon / \mathrm{d}$
Moody chart


Fig 5. Stanton Diagram

Experiment No. 9
Calculation and Data Sheet

Diameter of pipe $1 \mathrm{D}_{1}=$ $\qquad$
Diameter of pipe $2 D_{2}=$ $\qquad$
Area of pipe $1, \mathrm{~A}_{1}=$ $\qquad$
Area of pipe 2, $\mathrm{A}_{2}=$. $\qquad$
Volume of water $\mathrm{V}=$ $\qquad$
Collection time $\mathrm{t}=$ $\qquad$
Discharge= $\qquad$

| No <br> of <br> Obs. | Velocity <br> $\mathrm{V}_{1}$ | Velocity <br> $\mathrm{V}_{2}$ | $\mathrm{H}_{1}$ | $\mathrm{H}_{2}$ | Head loss <br> due to <br> Contraction <br> $\mathrm{H}_{\mathrm{LC}}$ | Head loss <br> due to <br> expansion <br> $\mathrm{H}_{\mathrm{LE}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |


| No. of observation |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- |
| Velocity $\mathrm{V}_{1}$ |  |  |  |  |  |
| Velocity $\mathrm{V}_{2}$ |  |  |  |  |  |
| Head loss due to <br> contraction $\mathrm{H}_{\mathrm{LC}}$ |  |  |  |  |  |
| Head loss due to <br> expansion $\mathrm{H}_{\mathrm{LE}}$ |  |  |  |  |  |

## Loss due to Elbows:

Diameter of pipe $\mathrm{D}=$
Area of pipe, $\mathrm{A}=$.
Relative roughness, $\varepsilon / \mathrm{D}=$ $\qquad$
Reynolds Number, $\mathrm{Re}=\mathrm{VD} / \mathrm{v}=$ $\qquad$
Volume of water $\mathrm{V}=$ $\qquad$
Collection time $\mathrm{t}=$
Discharge, $\mathrm{Q}_{\mathrm{a}}=$.

| $\begin{gathered} \text { No } \\ \text { of } \\ \text { Obs. } \end{gathered}$ | $\begin{aligned} & \text { Velocity } \\ & \quad \text { V } \\ & (\mathrm{cm} / \mathrm{sec}) \end{aligned}$ | $\mathrm{H}_{1}(\mathrm{~cm})$ | $\mathrm{H}_{2}(\mathrm{~cm})$ | Total head $\begin{gathered} \text { loss } \\ \mathrm{h}_{\mathrm{L}}=\mathrm{H}_{1}-\mathrm{H}_{2} \\ (\mathrm{~cm}) \end{gathered}$ | Friction factor, f' | Head loss <br> due to <br> Friction <br> $\mathrm{h}_{\mathrm{f}}(\mathrm{cm})$ | Head loss due <br> to elbows, $h_{\text {elbows }}$ (cm) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

## References

1. Daugherty, R.L., Franzini, J.B. and Finnemore, E.J., Fluid Mechanics with Engineering Applications, McGraw-Hill Book Co, Singapore-1989.
2. Department of Water Resources Engineering, Bangladesh University of Engineering and Technology, Fluid Mechanics Sessional.

## Appendix 1 <br> Lab Report Format

1. All students must have a same colored printed cover page. The design of cover page is provided with the lab manual. Students have to compose only the course teacher's name and designation and their information.
2. An index is provided. It should be printed and set after the cover page. Table may be filled up by pen during each submission after that particular subject has been covered.
3. Each report must have a common top page. Only the experiment name and no. and the date may be filled up by pen. A top page design is provided.
4. A4 papers have to be used for preparing the lab report.

## CE 272 <br> Fluid Mechanics Sessional (Lab Report)


Prepared For
Name of Course Teacher
Designation of Course Teacher
$\&$
Name of Course Teacher
Designation of Course Teacher

Prepared By
Name of Student
Student's ID
Year/ Semester
Group

Designation of Course Teacher

## INDEX

| Topic no. | Topic Name | Date of <br> Submission | Signature | Comments | Page no. |
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